



Philadelphia University
Faculty of Engineering

Student Name:
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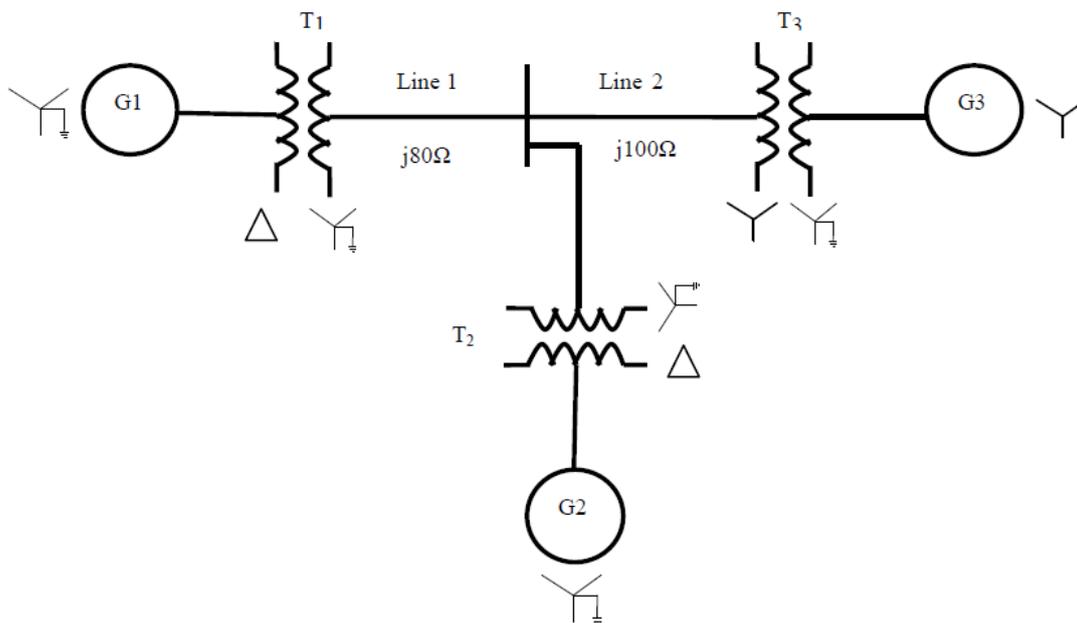
Dept. of Electrical Engineering
Final Exam, Second Semester: 2016/2017

Course Title: Power Systems I	Date: 12/6/2017
Course No: (610411)	Time Allowed: 2 Hours
Lecturer: Dr. Mohammad Abu-Naser	No. of Pages: 2

Question 1: (10 Marks)

Objectives: This question is related to single line diagram and per unit system

Draw the reactance diagram using a base of 50MVA and 13.8KV on generator G₁



- G1: 20MVA, 13.8kV, X=0.2
- G2: 30MVA, 18.0kV, X=0.2
- G3: 30MVA, 20.0kV, X=0.2
- T1: 25MVA, 220/13.8 kV, X =0.1
- T2: 3Single phase unit each rated 10MVA, 127/18 kV, X =0.1
- T3: 35MVA, 220/22 kV, X =0.1

Question 2: (10 Marks)

Objectives: This question is related to performance of transmission line

A 16-km three phase line has a series impedance $z = 0.125 + j0.4375 \Omega/\text{km}$. The line delivers 120 MVA at unity power factor at 64 kV. Calculate:

- 1) ABCD parameters of the transmission line
- 2) Sending end voltage and current (V_s and I_s)
- 3) Sending end power
- 4) Transmission line efficiency
- 5) Percent voltage regulation

QUESTIONS 3,4,5 ARE BASED ON THE FOLLOWING SINGLE-LINE DIAGRAM

Synchronous generators:

G1: $X_1=X_2=0.2$, $X_0=0.05$ pu

G2: $X_1=X_2=0.2$, $X_0=0.05$ pu

Transformers:

T1: $X=0.05$ pu

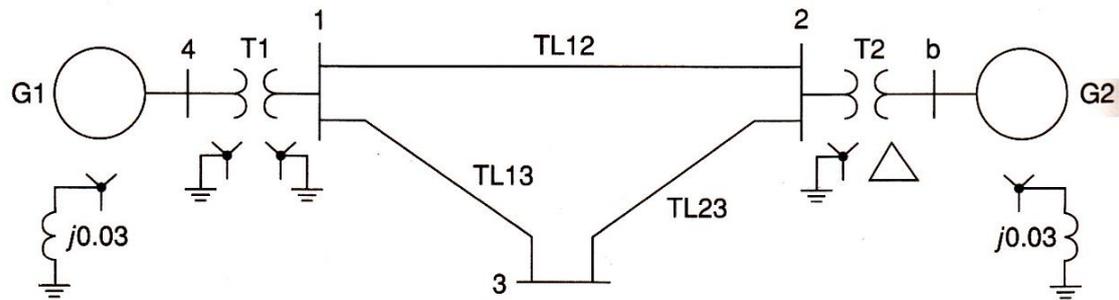
T2: $X=0.05$ pu

Transmission lines:

TL12: $X_1=X_2=0.1$, $X_0=0.3$

TL13: $X_1=X_2=0.1$, $X_0=0.3$

TL23: $X_1=X_2=0.1$, $X_0=0.3$



Question 3: (10 Marks)

Objectives: This question is related to sequence networks

- 1) Draw the per-unit positive, negative, and zero sequence networks.
- 2) Determine the Thevenin equivalent of each sequence network as viewed from bus 3.

Question 4: (5 Marks)

Objectives: This question is related to symmetrical fault analysis

- 1) Determine the positive sequence fault current $I_a^{(1)}$ for a bolted three phase fault at bus 3.
- 2) Determine the phase currents I_a , I_b , I_c .

Question 5: (5 Marks)

Objectives: This question is related to unsymmetrical fault analysis

Determine the fault current for a bolted double line-to-ground fault at bus 3.

Good luck

Power Systems (1)
Final Exam, Second Semester 2016/2017
Model Answers

Question 1

$$G_1: X = 0.2 \times \frac{50}{20} = .5 \quad \textcircled{1}$$

$$G_2: X = 0.2 \times \frac{50}{30} = .3333 \quad \textcircled{1}$$

$$G_3: X = 0.2 \times \frac{50}{30} \times \left(\frac{20}{22}\right)^2 = .2755 \quad \textcircled{1}$$

$$T_1: X = 0.1 \times \frac{50}{25} = .2 \quad \textcircled{1}$$

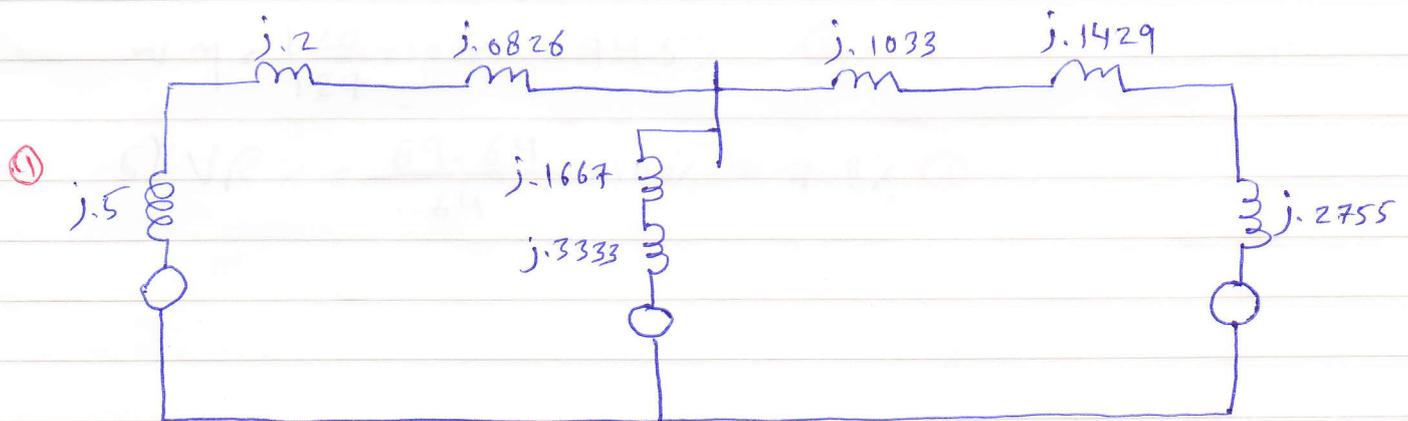
$$T_2: X = 0.1 \times \frac{50}{30} = .1667 \quad \textcircled{1}$$

$$T_3: X = 0.1 \times \frac{50}{35} = .1429 \quad \textcircled{1}$$

$$Z_{base} = \frac{220^2}{50} = 968 \, \Omega \quad \textcircled{1}$$

$$\text{Line 1: } X = \frac{80}{968} = .0826 \quad \textcircled{1}$$

$$\text{Line 2: } X = \frac{100}{968} = .1033 \quad \textcircled{1}$$



Question 2

$$1) Z = 16 (0.125 + j.4375) = 2 + j7 \quad (1)$$

$$A = 1 \quad (1.5)$$

$$B = Z = 2 + j7 \quad (1.5)$$

$$C = 0 \quad (1.5)$$

$$D = 1 \quad (1.5)$$

$$2) V_R = \frac{64}{\sqrt{3}} = 36.9504 \angle 0^\circ \text{ kV} \quad (1.5)$$

$$I_R = \frac{S_R}{3V_R^*} = \frac{120 \text{ MVA}}{3 \times 36.9504} = 1082.5 \angle 0^\circ \text{ A} \quad (1)$$

$$V_s = V_R + Z I_R \\ = 36.9504 \angle 0^\circ + (2 + j7) \times 1082.5 \times 10^{-3} \\ = 39.84 \angle 10.96^\circ \text{ kV} \quad (1)$$

$$V_{sLL} = 39.84 \times \sqrt{3} = 69 \text{ kV} \quad (1.5)$$

$$I_s = I_R = 1082.5 \angle 0^\circ \text{ A} \quad (1)$$

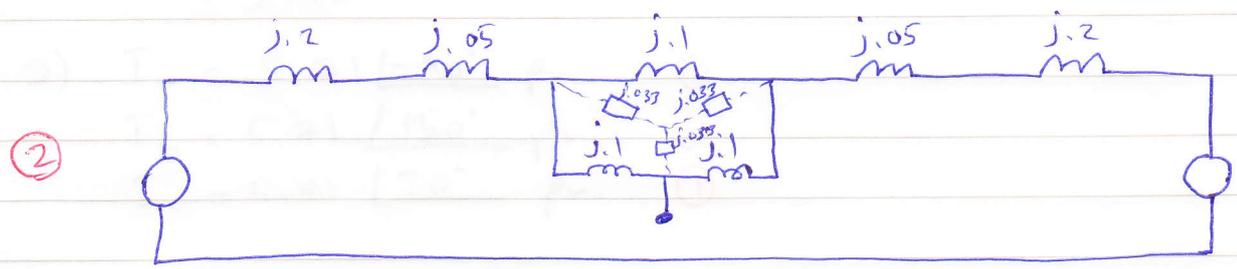
$$3) S_s = 3V_s I_s^* = 127 + j24.6 \text{ MVA} \quad (1)$$

$$4) \eta = \frac{120}{127} \times 100\% = 94.5\% \quad (1)$$

$$5) V_R\% = \frac{69 - 64}{64} \times 100\% = 7.8\% \quad (1)$$

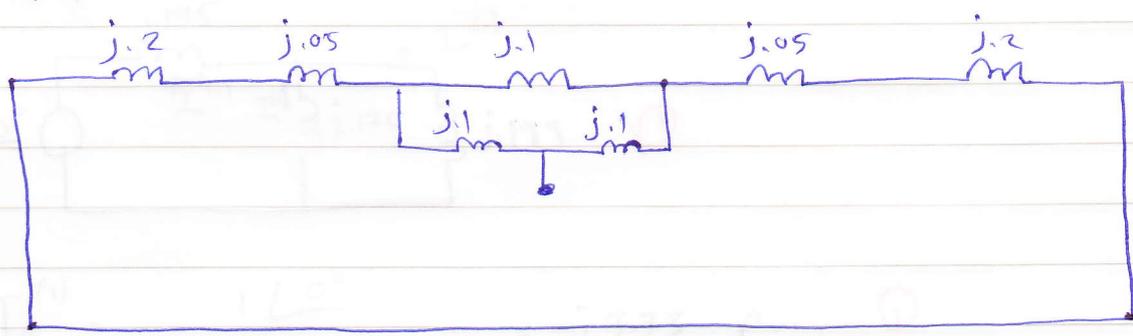
Question 3

1) +ve seq. net.



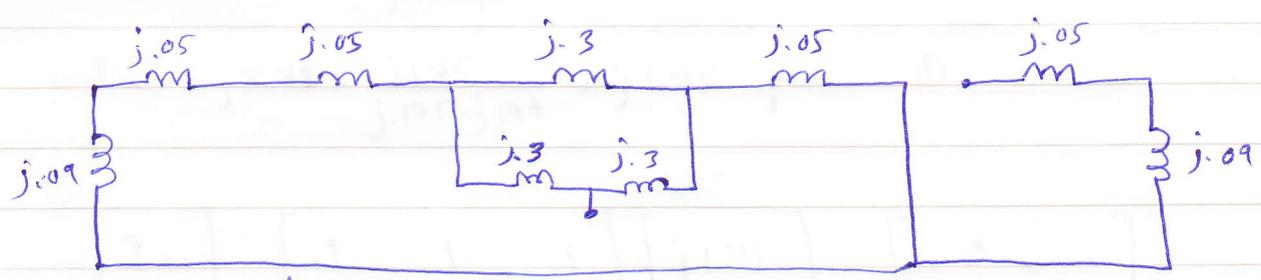
②

-ve seq. net.



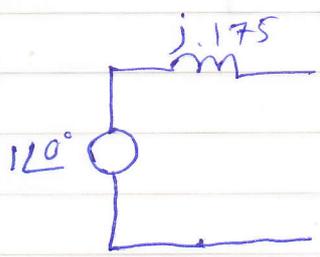
①

zero seq. net.

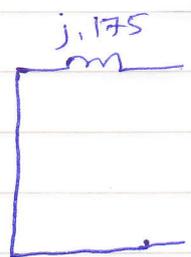


②

2) Using $\Delta-Y$ transformation and series-parallel combinations, Thevenin equivalents looking into bus 3 are:



+ve
②



-ve
①
-3-



②

Question 4

$$1) I_a^{(1)} = \frac{1 \angle 0^\circ}{j.175} = -j 5.71 \text{ pu} \quad (2)$$

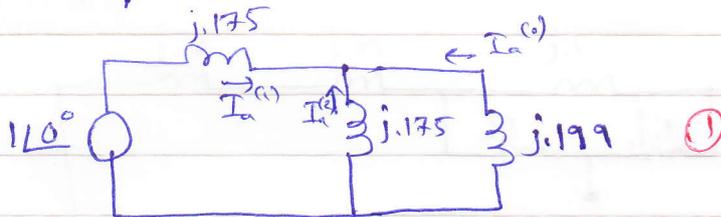
$$2) I_a = 5.71 \angle -90^\circ \text{ pu} \quad (1)$$

$$I_b = 5.71 \angle 150^\circ \text{ pu} \quad (1)$$

$$I_c = 5.71 \angle 30^\circ \text{ pu} \quad (1)$$

Question 5

The sequence network interconnection is shown below



$$I_a^{(1)} = \frac{1 \angle 0^\circ}{j.175 + j.175 \parallel j.199} = -j 3.73 \text{ pu} \quad (1)$$

$$I_a^{(2)} = j 3.73 \times \frac{j.199}{j.175 + j.199} = j 1.99 \text{ pu} \quad (1)$$

$$I_a^{(0)} = j 3.73 \times \frac{j.175}{j.175 + j.199} = j 1.75 \text{ pu} \quad (1)$$

$$\begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & a^2 & a \\ 1 & a & a^2 \end{bmatrix} \begin{bmatrix} j 1.75 \\ -j 3.73 \\ j 1.99 \end{bmatrix} = \begin{bmatrix} 0 \\ 5.6 \angle 152.1^\circ \\ 5.6 \angle 27.9^\circ \end{bmatrix} \quad (1)$$